# Faithful Completion of Images of Scenic Landmarks using Internet Images

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Abstract—Previous works on image completion typically aim to produce visually plausible results rather than factually correct ones. In this paper, we propose an approach to *faithfully* complete the missing regions of an image. We assume that the input image is taken at a well-known landmark, so similar images taken at the same location can be easily found on the Internet. We first download thousands of images from the Internet using a text label provided by the user. Next, we apply two-step filtering to reduce them to a small set of candidate images for use as source images for completion. For each candidate image, a co-matching algorithm is used to find correspondences of both points and lines between the candidate image and the input image. These are used to find an optimal warp relating the two images. A completion result is obtained by blending the warped candidate image into the missing region of the input image. The completion results are ranked according to combination score, which considers both warping and blending energy, and the highest ranked ones are shown to the user. Experiments and results demonstrate that our method can faithfully complete images.

Index Terms—Image Generation, Image Completion, Image Matching, Image Blending.

## **1** INTRODUCTION

There is strong public demand to repair photographs, for example to remove an unwanted object or person from a wedding or travel photo, or to fill missing areas in an old, damaged photo. Image completion provides an effective tool for this purpose. It fills in missing or unwanted regions with new plausible content.

Image completion has been widely investigated in the computer graphics and image processing communities. One category of existing methods [1], [2], [3] fills missing regions using content from the same input image, based on texture and patch similarity. Recent Internet-based image completion work [4], [5] takes visual fidelity of image completion to a new level. Instead of searching within the input image, holes are filled by finding suitable image regions in a huge image database. While existing work is able to produce visually plausible results, they are usually not a *faithful* reconstruction of the real objects or scene that should have been there.

In this paper, we propose an image completion approach which aims to faithfully reconstruct a correct image. We assume that the input image was taken at a famous scenic landmark, and that a text label describing or naming the landmark is also given. We download thousands of images by searching the Internet using the text label, after which two-step filtering is applied to obtain a small set of candidate images from amongst the downloaded images. Specifically, we only retain candidates which are similar to the input image in gist feature space [6] and which are well registered with the input image. Thus, the candidate

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images generally contain the same scene as the input image, but taken with different camera parameters, from different viewpoints, or under different illumination conditions.

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For each candidate image, in order to utilize it for completion, we need to align it with and warp it to the input image. To do so, we use a co-matching algorithm, which finds both point and line correspondences between the candidate image and the input image. Then, we adopt a mesh based warping strategy, and use a carefully designed energy function to preserve both point and line correspondences, and shapes. This energy is minimised iteratively. The completion result is obtained by blending the warped candidate image into the missing region of the input image. An optimal seam is found using graph-cut and blending is done in the gradient domain. Multiple completion images are generated, and the ones with the highest scores which consider both warping and blending energy are then returned to users. Experiments and results demonstrate that our method can effectively generate faithful completion images.

In summary, our work has three main contributions:

- A fully automatic approach to faithfully complete images of scenic landmarks. Previous approaches to this problem are not fully automatic [7] or cannot handle such complex cases [8] as our approach.
- A co-matching technique which, when matching line segments, utilizes geometric information from previously matched points. It is more efficient than the state-of-the-art line matching technique.
- A warping technique that can well register two images of non-planar scenes. The images may be taken from different viewpoints, under different illuminance conditions and with different lens distortions.

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## 2 RELATED WORK

**Image Completion.** Image completion approaches can be classified into diffusion based and example based approaches. Diffusion based methods [9], [10], [11] aim to extend image structures into small holes, and so cannot deal with large missing regions. Recent work has mainly focused on example based methods. Texture synthesis methods [12], [1] are example-based and perform well on images with holes in textured regions. The bottleneck lies in finding patch correspondences, which is time consuming. PatchMatch [2] utilizes the observation that neighbours of matched patches are also likely to be matched to significantly accelerate the process. Generalized PatchMatch [13] further improves PatchMatch by taking scaling and rotation of patches into consideration. Darabi et al. [14] improved the algorithm of Wexler et al. [1] in two ways: they calculate transformations of patches rather than only shifts of patches using the Generalized PatchMatch algorithm, and they add patch gradients in their distance metric in addition to colors. They also explored a similar multi-image completion process which fills a hole in one image with contents from other images. They adopted a *voting* strategy for visually plausible completion while we use a warping strategy for faithful completion. Furthermore, their candidate image is manually selected while ours is automatically selected. Sun et al. [15] proposed a structure-preserving image completion method which allows users to label structural information with lines. As well as line structures, other types of structures like symmetric structures [16] and planar structures [17] are also used to guide image completion. More recently, various automatic approaches have been proposed to analyse structural information both within images [18], [19] and between non-overlapping image pieces [20]. He et al. [18] compute the statistics of patch offsets automatically and formulate the completion process as a photomontage problem [21]. Huang et al. [19] detect planar surfaces and regularities within images and use them to guide patch search.

Some methods have considered faithful image completion [8][7] or faithful image expansion [22], i.e. showing visually correct content corresponding to the actual scene. They rely on images taken from similar viewpoints, and need to align these images to the viewpoint of the input image. A homography relates two images of the same scene taken from two different viewpoints if the scene is planar. Amirshahi et al. [8] use a single homography calculated by matching SIFT points to transform the candidate image to the input image: their method is thus limited to near-planar scenes. Whyte et al. [7] observed that non-planar scenes can be approximated by several planes, so they group homographies using matched SIFT points and transform the segmented planar regions with different homographies. Since segmenting an image into several planar regions is challenging, their method requires user intervention to obtain a correct segmentation, so is not automatic. Shan et al. [22] calculate structure from motion and reconstruct perview depth-maps to warp each candidate image to the input image. As in [7], they have to solve a labeling problem to decide which warped image each pixel should come from. Such methods, which compose holes from multiple source images, all suffer from artifacts due to incompatibility of the warped sources. Our approach is superior, in that it gives a plausible warp relating two different view images in 2D, based on robust point and line matching.

**Internet Image Processing.** In recent years, researchers have developed many Internet-based techniques for e.g. scene completion [4], city reconstruction [23], photo enhancement [24] and image montage synthesis [25]. Such works construct a large database by downloading millions of images from the Internet, and use this as a data source for different image processing tasks. Our work also belongs to this category. A detailed survey can be found in [26].

Point Correspondences. Approaches for finding point correspondences in images can be classified as providing sparse correspondences [27], [28], [29], [30] or dense correspondences [31], [32]. Finding point correspondences is also referred to as keypoint matching. One of the most popular keypoint descriptors is SIFT [27], and in many cases, SIFT matches are used as initial correspondences. To filter out wrong matches, Cho et al. [28] cluster the initial matches based on their geometric distances and discard small clusters as outliers. In cases where a non-rigid mapping exists, an alternative approach is to model the correspondence problem as a graph matching problem [29]. Spectral techniques [30] and geometric blur descriptors [33], [34] have also been used for keypoint matching. Calculating dense correspondences is more challenge than calculating sparse correspondences. HaCohen et al. [31] proposed a patch based approach. They first calculate the nearest neighbour field by Generalized PatchMatch[13]; each patch is related to its nearest neighbour by a transformation. Two neighbourhood patches are regarded as consistent if the transformations to their nearest neighbours are similar. They link consistent patches to get dense correspondence. Another way to calculate dense correspondences is to use pixel based algorithms. Instead of using pixel intensities to calculate optical flow [35], Liu et al. [32] extract SIFT descriptors for each pixel thus extending frame-by-frame optical flow to scene-level image correspondences.

Line Correspondences. Various work has also been proposed for finding line correspondences [36], [37], [38], [39]. A straightforward approach is to use local features to describe line segments [37]. They calculate the histogram of gradient along a line segment, and use this as the descriptor for line segments. It is easy to extend this descriptor to curved lines. Another strategy is to use matched points to boost line matching [36]. In this work, Fan et al. observed that for two keypoints on the same side of a line, the ratio of their distances to the line is an affine invariant, which can be utilized to check if two lines match. A more reasonable way is to use epipolar geometry to register lines [39], but this requires camera calibration beforehand.

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Image Warping. Warping is an efficient tool for image manipulation. Many works [40], [41], [42] generate control meshes in an image and define different forms of energy functions to optimize the positions of mesh vertices. These energy functions are application specific. To warp a panorama from an irrelugar shape to a rectangle, He et al. [40] consider shape preservation, straight line preservation and boundary constraints to optimize the guiding mesh. Carroll et al. [41] use shape preservation, straight line preservation and smoothness terms to constrain warping, thus making a wide-angle image look more friendly to human eyes. In video stabilization, Liu et al. [42] smooth the trajectory of a camera and project the original vertices into new positions. In their energy term, saliency and temporal coherence are also considered besides the commonly used similarity transformation term.

## **3** OVERVIEW

We take as input a scenic landmark image associated with a text label. Our approach consists of four steps; the pipeline of our approach is illustrated in Figure 1.

- Candidate Image Downloading and Pre-Processing. We download several thousand images by searching flickr.com using the associated text label. Following [4], we use gist scene descriptors [6] to perform initial filtering. The closest one hundred images to the input image according to gist scene descriptors are retained.
- Candidate Images Filtering. Next, the candidate images are reduced to a small set (typically 20) based on registration scores (Section 4). These images should contain the same scene as the input image, and can potentially produce good completion results. For each candidate image, we generate a completion image in the next step.
- Co-Matching, Warping and Blending. We first detect key points in both the candidate image and the input image, and find matches between the key points using agglomerative correspondence clustering [28]. A homography is computed for each cluster of matches. Line segments are also extracted in both images using [43]. To obtain better line matching results, we extend MSLD [37] by taking homographies recovered from point matching into consideration. Details are explained in Section 5. Next, we need to warp the candidate image to the input image. To do so, we adopt a mesh based warping strategy, using an energy function which preserves both point and line correspondences found in the co-matching step, as well as line structures and shapes. The energy function is minimized iteratively, as shown in Section 6. An example showing part of a candidate image before and after warping can be seen in Figures 2(a) and (b). To obtain a completion image, we need to blend the warped candidate image into the missing region of the input image. We first obtain an optimal seam

using graph cut [44] (see Figure 2(c)), and then use the algorithm in [45] to blend the candidate image into the input image.

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• **Ranking.** The above process provides multiple completion images. For each result, we compute a combination score, which considers both warping and blending energy. The completion images with the highest combination scores are returned to the user.

## 4 CANDIDATE IMAGE FILTERING

To achieve faithful image completion, we need to use content from other images which contain the same scene as the input image. To do so, we first download several thousand images from Flickr using the text label associated with the input image. As most of the downloaded images are unrelated to the input image, we use gist scene descriptors [6] with 8 orientations and 4 scales to discard dissimilar images. The candidate images after initial filtering are denoted by  $S_g$  (their number is denoted  $N_g$ ). Next, we need to find which candidate images contain the same content as the input. For this purpose, we define a registration score for each candidate image, which measures how well it can be registered to the input image. The  $N_p$  candidate images with highest registration scores are then retained and passed to further steps. The registration score P is defined as:

$$P(I_s, I_t) = \lambda_m \frac{P_m(I_s, I_t)}{\max(P_m(I_s, I_j))} - \lambda_a \frac{P_a(I_s, I_t)}{\max(P_a(I_s, I_j))}, \quad (1)$$

where  $I_j$  is from  $S_g$ ,  $I_t$  denotes the candidate image, and  $I_s$  denotes the input image. The registration score involves two terms: the point matching term  $P_m$  and the affine registration term  $P_a$ . These terms are weighted by  $\lambda_m$  and  $\lambda_a$ , and are divided by their maximal values for normalization, respectively. The point matching term  $P_m$  is defined as:

$$P_m(I_s, I_t) = |C_{s,t}| \tag{2}$$

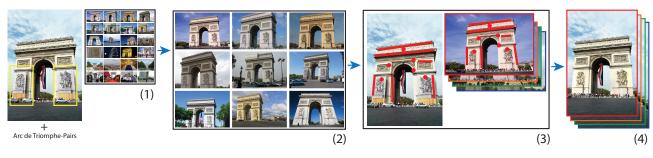
where  $|C_{s,t}|$  denotes the number of point matches between the input image  $I_s$  and the candidate image  $I_t$ . Details of point matching are presented in Section 5. The affine registration term  $P_a$  is defined as:

$$P_{a}(I_{s}, I_{t}) = \frac{\sum_{(x_{s}, x_{t}) \in C_{s,t}} \|A_{t}x_{t} - x_{s}\|}{B}$$
(3)

where *B* denotes the size of a bounding box that contains all matching points, and  $A_t$  is the optimal affine transformation matrix that matches all points from the input image to the candidate image, which is obtained using the algorithm in [46].

In our implementation, we empirically set the weights  $\lambda_m = 2$  and  $\lambda_a = 1$ . The number of retained images after initial filtering is set to  $N_g = 100$ , and the number of final retained candidate images is set to  $N_p = 20$ . Our experiments show that this setting gives a good balance between speed and accuracy. Our Matlab implementation takes about 400 seconds for this step (not including the time to download images).

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Candidate Image Downloading and Pre-Processing

Candidate Images Filtering

Co-Matching, Warping and Blending

Ranking

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Fig. 1. Pipeline. (1) The input is a source image of a famous landmark, plus a keyword describing it. Image search engines are used to download initial candidate images. Gist descriptors are used to filter the initial image set. (2) We select potential candidates by further filtering. (3) For each candidate image, we match points and line segments, and compute an optimized warp from the candidate image to the source image. We then cut the appropriate part from the candidate image and blend it into the source image. (4) A ranking function is used to select the best completion results.



Fig. 2. (a) Part of the candidate image. (b) Warped result.(c) Optimal seam (blue).

## 5 CO-MATCHING

The previous section explained how to obtain a small set of candidate images. These candidate images generally contain the same scene as the input image, but taken with different camera parameters, at different viewpoints or under different illumination conditions. Now, we need to find correspondences between each candidate image and the input image, in order to align them later. Various work has been proposed for finding point correspondences [27] and line correspondences [36] between two images. In order to obtain more robust matching results, we have developed a co-matching algorithm, which finds both point and line matches. The main idea is to use the recovered homography based on point correspondences to further improve the accuracy of line correspondences. The comatching algorithm works as follows:

**Point Correspondences.** We first detect MSER regions [47] and extract SIFT [27] features to match the key points of the two images. Next, we cluster the matched points based on the feature distance between each matched point pair. We adopt agglomerative correspondence clustering [28] to cluster the matched pairs and discard small clusters (with less than 20 pairs) as outliers. Then, we compute a homography by least-squares fitting for each remaining cluster. A recovered homography is illustrated in Figure 4.

**Line Correspondences.** First, we use the method of [43] to detect line segments in both images (see Figure 3). To match line segments between two images, we need a distance metric for line segments. We use:

$$D(l_i, l_j) = D_{\text{feat}}(l_i, l_j) + \alpha D_{\text{geo}}(l_i, l_j), \qquad (4)$$

where  $l_i$ ,  $l_j$  are line segments in the two images respectively. Our distance metric takes two terms into account: the feature distance  $D_{\text{feat}}$  and the geometric distance  $D_{\text{geo}}$ .  $\alpha$ is a weight to control the relative contributions of the two terms, set to  $\alpha = 2$  empirically. The feature distance  $D_{\text{feat}}$ is computed as the difference of the MSLD descriptors [37] of the two line segments. The geometric distance measures how well the two line segments match each other under the homography just recovered, and is defined as:

$$D_{\text{geo}}(l_i, l_j) = \frac{1}{2} (D_{\text{Hough}}(H_i l_i, l_j) + D_{\text{Hough}}(H_j^{-1} l_j, l_i)), \quad (5)$$

where  $D_{\text{Hough}}$  represents the distance of two lines in Hough space;  $H_i$  and  $H_j$  are homographies at  $l_i$  and  $l_j$ , respectively, which have been recovered in the previous point matching step. Both feature and geometric distances are normalized to [0, 1] by dividing by their maximal values, respectively.

nography by least-squares fitting for each We then use the line distance metric in Equation 4 to compute all-pair distances between line segments in the 1077-2626 (c) 2015 IEEE. Personal use is permitted, but republication/redistribution requires IEEE permission. See

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Fig. 3. Line detection. Blue lines show detected line segments whose length is at least 40 pixels.



Fig. 4. Homography region partition. Matched points in the same cluster are marked in the same color. For each cluster, we fit a homography based on the matched points.

two images. Two line segments  $l_i$  and  $l_j$  are considered as matched if  $l_i$  is closest to  $l_j$  among all line segments in the input image, and  $l_j$  is also closest to  $l_i$  among all line segments in the candidate image.

Evaluation. To evaluate the effectiveness of our comatching algorithm, we compared it to two state-of-theart line matching algorithms: Fan's algorithm [36] and Wang's algorithm [37]. To enable a fair comparison, all the algorithms should have a similar number of matched lines. In some cases we should increase the number of matched lines for a certain algorithm while decrease the number of matched lines for another algorithm. To increase the number of matched lines, we loosened the matching criteria for the algorithm: two line segments from two images are matched if they belong to each other's top n matches where *n* is a parameter. To decrease the number of matched lines, we set a distance threshold t to discard some matched line pairs whose distances are larger than t. We adjusted n and t to let these algorithms have a similar number of matched lines. The lines were generated using the method in [43], and used as input for all 3 algorithms. As shown in Table 1, our line matching algorithm has a higher correct matching rate than these previous methods.

## 6 WARPING CONSTRAINED BY POINTS AND LINES

After finding point and line matches between the input image and the candidate image, the next tasks are to align the matched points and lines, and to warp the candidate image to the input image. To do so, we adopt a mesh-based warping algorithm with a carefully chosen energy function. We parameterize the candidate image using a uniform mesh with  $20 \times 20$  vertices. The energy function considers constraints on both point and line correspondences, as well as preserving shape and line structures. In the following, we explain the details of the energy function, and how we use the mesh grid for warping.

#### 6.1 Energy Function

Our energy function considers constraints on matched points and lines, as well as preserving structures like shapes and other straight lines. We denote the initial mesh by  $\hat{V}$ , and the output optimized mesh as V. The vertices of the grid V are denoted by its x- and y- coordinates:  $V = \{(x_i, y_i), 1 \le i \le N\}$ , where N is the number of vertices.  $\hat{V}$  is defined in a similar way.

**Point Constraints.** The point constraint term constrains the matched points to remain close after warping. Specifically, the point constraint term  $E_P$  is defined as:

$$E_P(V) = \sum_{i=1}^{K} (x_{i,s} - x_{i,r})^2 + \sum_{i=1}^{K} (y_{i,s} - y_{i,r})^2, \qquad (6)$$

where *K* is the number of matched point pairs;  $(x_{i,s}, y_{i,s})$  and  $(x_{i,r}, y_{i,r})$  are the positions of the points of the *i*-th matched pair (subscripts *s* and *r* represent the input and warped candidate images, respectively). Note that the position of each point in the warped candidate image is found by bilinear interpolation of its four adjacent vertexes, so that  $E_P$  can be written as a quadratic function of vertex positions *V*.

**Line Constraints.** Since human vision is very sensitive to artifacts along straight lines, we also wish to preserve line correspondences during warping. We constrain the lines in the warped candidate image to have similar orientations and positions to the corresponding lines in the input image, and to remain straight. We use two terms  $E_{LC1}$  and  $E_{LC2}$  to impose line constraints, which preserve orientation and position of lines, respectively. Denote the lines in the input and the warped candidate image as  $l_{i,s}$  and  $l_{i,r}$ , respectively. Inspired by [48], we cut a line segment into smaller segments if it crosses mesh edges.

For each line segment in a mesh quad, its orientation vector is computed as the direction from one endpoint to the other. For each matched pair of line segments, we denote the orientation vector of the line segment in the input and warped candidate images as  $\hat{e}$  and e, respectively. The first term  $E_{LC1}$  is defined as the mean distortion over all segments:

$$E_{LC1}(V) = \frac{1}{N_{LC}} \sum_{i=1}^{N_{LC}} \|s_i R_i \hat{e}_i - e_i\|^2,$$
(7)

where  $N_{LC}$  is the number of segments,  $R_i = \begin{pmatrix} \cos \theta_i & -\sin \theta_i \\ \sin \theta_i & \cos \theta_i \end{pmatrix}$  is a rotation matrix, and *s* is a scaling factor. Unlike in [48], here the rotation angle  $\theta_i$  is given by the matched line pair with index *i*. Minimizing this energy term with respect to *s* gives:  $s = (\hat{e}^T \hat{e})^{-1} \hat{e}^T R^T e$ . Since *e* can be represented by a linear function of *V*,  $E_{LC1}$  can also be written as a quadratic function of *V*.

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total matched lines correct match correct rate time(s) source image candidate image Fan's method 108 102 94% 16 77% 106 Kensington Castle Wang's method 82 5 98% 1000\*667 1504\*1000 Our method 103 101 16 29 Fan's method 135 108 80% Notre Dame Wang's method 125 107 85% 4 99% 15 1000\*928 Our method 140 139 922\*1229 Fan's method 198 182 92% 22 Duomo Wang's method 194 87% 4 168 202 93% 8 1000\*664 1000\*709 188 Our method Fan's method 266 256 96% 32 Palazzo Santa Sofia Wang's method 255 91% 6 278 243 235 97% 15 1024\*632 1024\*768 Our method 159 97% 5 Fan's method 164 Rialto Bridge Wang's method 86% 3 133 114 Our method 152 148 97% 5 820\*403 820\*403 Fan's method 40 35 88% 6 Leaning Tower of Pisa Wang's method 32 27 84%  $\overline{2}$ Our method 35 32 91% 6 684\*1024 683\*1024 Fan's method 99% 7 138 137 Arc de Triomphe -Paris 4 Wang's method 162 139 86% Our method 146 146 100% 6 533\*800 968\*667 Fan's method 44 30 68% 4 Big Ben Wang's method 43 32 74%3 Our method 45 41 91% 4 1024\*683 685\*1024

TABLE 1 Line matching: our results compared to Fan's algorithm and Wang's algorithm.

The second term  $E_{LC2}$  is designed to constrain the position of lines. Inspired by [48], we transform a line y = ax + b in image space into a point  $(r, \theta)$  in Hough space. For an arbitrary point  $(x_0, y_0)$  on this line,  $x_0 \cos \theta + y_0 \cos \theta = r$ . We constrain the range of  $\theta$  to be  $[0, 2\pi)$ , so that rwill always be positive. For each segment in a quad, we denote its final position after warping as  $(r_i, \theta_i)$  in Hough space. Meanwhile, we also know its ideal position  $(\hat{r}_i, \hat{\theta}_i)$ according to the corresponding line in the source image. To simplify the problem, we suppose that  $\theta_i$  is always equal to  $\hat{\theta}_i$ , so that  $r_i$  is the only unknown and can be represented by a linear combination of the four quad vertexes. This assumption is reasonable provided we give a large weight to  $E_{LC1}$ . Now the second line constraint term  $E_{LC2}$  can be defined as:

$$E_{LC2}(V) = \frac{1}{N_{LC}} \sum_{i=1}^{N_{LC}} \|\hat{r}_i - r_i\|^2.$$
(8)

 $E_{LC2}$  can also be rewritten as a quadratic function of V.

**Line Preservation.** Besides lines in correspondence, we also want to constrain all unmatched lines to be straight after warping. We define the line preservation term  $E_{LP}$  as:

$$E_{LP}(V, \{\boldsymbol{\theta}_m\}) = \frac{1}{N_{LP}} \sum_{i=1}^{N_{LP}} \|s_i R_i \hat{e}_i - e_i\|^2.$$
(9)

Unlike the line constraint term, here the rotation angle for each segment is also an unknown. Following [48], we quantize the orientation range into 50 bins. Each segment can be assigned to a bin according to its original orientation. We encourage segments in the same bin *m* to share the same rotation angle  $\theta_m$ . Actually, some of the  $\theta_m$  can be pre-computed. For a line with correspondence, we already know its rotation angle  $\theta$ . Then we can compute which bin it belongs to and fix the  $\theta_m$  for that bin as  $\theta$ . Meanwhile, the rotation angles of lines without correspondences will be guided by those with correspondences.

**Shape Preservation.** In order to preserve the shape of the image content, we define a shape preservation energy term as:

$$E_{\mathcal{S}}(V) = \frac{1}{N_q} \sum_{q=1}^{N_q} \| (A_q (A_q^T A_q)^{-1} A_q^T - I) V_q \|^2, \qquad (10)$$

where  $N_q$  is the number of quads in the mesh,  $A_q$  is defined as:

$$A_{q} = \begin{bmatrix} \hat{x}_{0} & -\hat{y}_{0} & 1 & 0\\ \hat{y}_{0} & \hat{x}_{0} & 0 & 1\\ \vdots & \vdots & \vdots & \vdots\\ \hat{x}_{3} & -\hat{y}_{3} & 1 & 0\\ \hat{y}_{3} & \hat{x}_{3} & 0 & 1 \end{bmatrix},$$
 (11)

and  $V_q$  is defined as:

$$V_q = [x_0, y_0, x_1, y_1, \dots, x_3, y_3]^T.$$
 (12)

Here we denote the four corners of the quad as  $(x_0, y_0), \ldots, (x_3, y_3)$ .  $E_S$  encourages each quad to undergo a similarity transformation; a detailed derivation can be found in [49].

**Total Energy Function.** Finally, the total energy function E is defined as:

$$E(V, \{\theta_m\}) = E_P + \lambda_{LC1}E_{LC1} + \lambda_{LC2}E_{LC2} + \lambda_{LP}E_{LP} + \lambda_{S}E_{S},$$
(13)

where each  $\lambda$  controls the weight of the corresponding term. Same as previous works [40], [41] we give high weight for line orientation term. In our implementation, we empirically set  $\lambda_{LC1}$  to 100000,  $\lambda_{LC2}$  to 1,  $\lambda_{LP}$  to 100,  $\lambda_{S}$  to 1000.

#### 6.2 Iterative Two-step Optimization

Minimizing the energy to find V and  $\{\theta_m\}$  in Equation 13 at the same time is difficult. Instead, we solve this problem using an iterative two-step approach. In the first step, we fix  $\{\theta_m\}$  and solve for V, making E a quadratic function which can be solved by a linear least-squares solver. Since we have only 400 vertexes in V (i.e. 800 unknowns), the linear system can be solved rapidly. In the second step, we fix V and solve for  $\{\theta_m\}$ . To simplify the problem, we use an intuitive averaging strategy instead of a non-linear solver. Specifically, each  $\theta_m$  can be estimated using the average of the relative angle between e and  $\hat{e}$  for all segments in the bin indexed *m*. However, not all elements in  $\{\theta_m\}$  should be updated. As mentioned in Section 6.1, the rotation angle  $\theta$  for a line with correspondence is already known and the related bin in  $\{\theta_m\}$  should be fixed to  $\theta$ . We iteratively apply the above two steps, and usually 5 iterations suffice to obtain a satisfactory result.

#### 7 RESULT RANKING

After obtaining one completion result for each candidate image, we now need to select the best results from those obtained. We define the score of a completion result as:

$$R = \lambda_r P(I_s, I_t) + \lambda_w P_w(I_s, I_t) + \lambda_g P_g(I_s, I_t)$$
(14)

where  $I_s, I_t$  denote the input and the corresponding candidate images, respectively;  $P(I_s, I_t)$  is the registration score defined in Section 4;  $P_w$  is the warping score and it is defined as:

$$P_{w}(I_{s}, I_{t}) = 1 - \frac{E_{w}(I_{s}, I_{t})}{\max(E_{w}(I_{s}, I_{j})), j \in S_{g}}$$
(15)

where  $E_w(\cdot, \cdot)$  is the total warping energy of the two images defined in Eqn. 13.  $P_g$  is the normalized energy of the graph-cut boundary segmentation:

$$P_g(I_s, I_t) = 1 - \frac{E_g(I_s, I_t)}{\max(E_g(I_s, I_j)), j \in S_g}$$
(16)

where  $E_g(\cdot, \cdot)$  is the graph-cut energy used in [21]. We add this term because a poorly segmented boundary always leads to obvious artifacts.

In our implementation, we empirically set the weights in the ranking function to  $\lambda_r = 0.2$ ,  $\lambda_w = 0.4$  and  $\lambda_g = 0.4$ , respectively. By default, our system returns the result with the highest score. Users can also select from further results if dissatisfied with the top ranked result. Various ranked results are illustrated in Figure 5.

#### 8 RESULTS AND DISCUSSION

#### 8.1 Implementation Details.

We have implemented our method using Matlab on a PC with an Intel Core i7 3.4GHz CPU and 8GB memory. Our system takes about 2 minutes to obtain the final completion results for a typical input image with  $1200 \times 800$  resolution (the time for downloading images is not included).

#### 8.2 Demonstration

Figure 6 demonstrates the effectiveness of our system, showing completion results for various scenes. In the first row, the input image (i.e. the left column) is taken at the Rialto Bridge in Venice. Notice that there is an unwanted flag in the middle of the bridge, occluding part of it. Our method successfully removed the flag and replaced it with content from other images. Our result is given in the right column; candidate images are shown in the middle column. Other rows show results at Kensington Palace (with an unwanted statue in front of the palace), at a bridge in a traditional Chinese town (with unwanted people), at a Buddhist temple in Japan (the bottom-left corner is occluded by a tree), and at the Leaning Tower of Pisa (one of the floors is covered by a fence). Our method can handle all these cases well.

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#### 8.3 Need for Both Point and Line Constraints

The reason we do co-matching is that both point constraints and line constraints play important roles in our warping. We illustrate this in Figure 7. In Figure 7(a), we want to remove the man in front of the Duomo of Milan. Without point constraints, the entire wall cannot be well registered: see Figure 7(b). When we add point constraints but not line constraints, although on the whole the result is better registered than in Figure 7(b), there is still severe misalignment in the line structures: see Figure 7(c). Figure 7(d) is the result using both point and line constraints. It is well registered and the completion result does not suffer from artefacts.

#### 8.4 Comparison with PatchNet and Scene Completion

We next compare our approach with state-of-the-art Internet based image completion methods including a scene completion method [4] and PatchNet [5]. To enable a fair comparison, we built an image library containing hundreds of thousands of images, and used same image library for all three methods. As shown in Figure 8, for all four examples, our method is able to generate faithful completion results, while the scene completion method [4] and PatchNet [5] both generate unfaithful (although visually plausible) results. This is unsurprising, since these two methods only find similar images (or similar content in images) and aim to generate *plausible* results. In comparison, our method uses images taken at the same scene for completion, and hence is more effective in generating *faithful* completion results.

### 8.5 Comparison with Moving Least-Squares Deformation

We now compare our warping method in Section 6 to moving least-squares deformation (MLSD) [50]. The candidate



Fig. 5. Ranked results, showing 4 representatives. Rank 1 is the best result; Rank 4 suffers from a non-smooth graph-cut boundary; Rank 9 has many fewer matching points; Rank 15 has too large a viewpoint difference.

image used was the same in both cases. MLSD uses point constraints as well as line constraints. With MLSD, too many point constraints lead to extreme distortion, so we picked 20 matched pairs with the highest confidence in our results. For similar reasons, we picked the 5 best matched lines. After deformation, we blended the deformed parts into the source image. In the first row of Figure 9, the clock of Big Ben was replaced. Neither point constraints nor line constraints can preserve local shapes. Compared with the results in the first row, the distortion in the deformation using MLSD is more obvious in the second row of Figure 9, where we tried to remove the boat in front of the Palazzo Santa Sofia.

### 8.6 Comparison with Single and Multiple Homography Approaches

Our approach is superior to the single homography approach in [8] and the multiple homography approach in [7]. A single homography cannot register the source image and the candidate image for non-planar scenes. Multiple homography suffer from incompatibility between the images due to different white balance, different resolution and different lighting conditions. In Figure 10, we compare our approach with single and multiple homography approaches. For the single homography approach, we use the same candidate image as in our approach. For the multiple homography approach, we use the top 10 images after initial filtering. In the first row, we remove the statue in front of St. Basil's Cathedral. Using the single homography approach, the left of the image is excessively stretched. The result of multiple homography approach seems good at first glance, but the blue and white top is doubled. In the second row, we remove the part of the central television building that is being built. The single homography approach fails to register the building well while this problem is less severe for the multiple homography approach. However, different parts coming from from different candidate images

leads to color inconsistency, which is the main artefact in this case. In the third row, we recover the occluded part of the Royal Albert Hall. The single homography approach again suffers from misalignment while for the multiple homography approach the bottom right statue is missing. In all the above cases, our approach generates faithful completion results. We give more comparisons in the supplemental material.

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#### 8.7 Depth of Field Extension

Our approach can also be used to change the depth of field of a photograph, producing interesting effects. In Figure 11, we replace the blurred objects with sharp ones to increase the depth of field.

#### 8.8 Limitations

Our method may fail in some cases. For example, if the viewpoint differs greatly between the input and candidate images, it may be hard to find a reasonable warp from the candidate image to the input image, leading to results with inconsistent alignment (see Figure 12, first row). Furthermore, if there are large tone and illumination differences between the input image and the candidate image, visible color inconsistency artifacts may result (see Figure 12, second row).

Another limitation of our approach is that it cannot handle cases when the target region is too large. This is because our approach relies on correspondences between two images outside the target region, and if the target region is too large, there will be few matches. The point and line terms of the energy function will have less impact so the optimization cannot give a reasonable warp (see Figure 12, third row).

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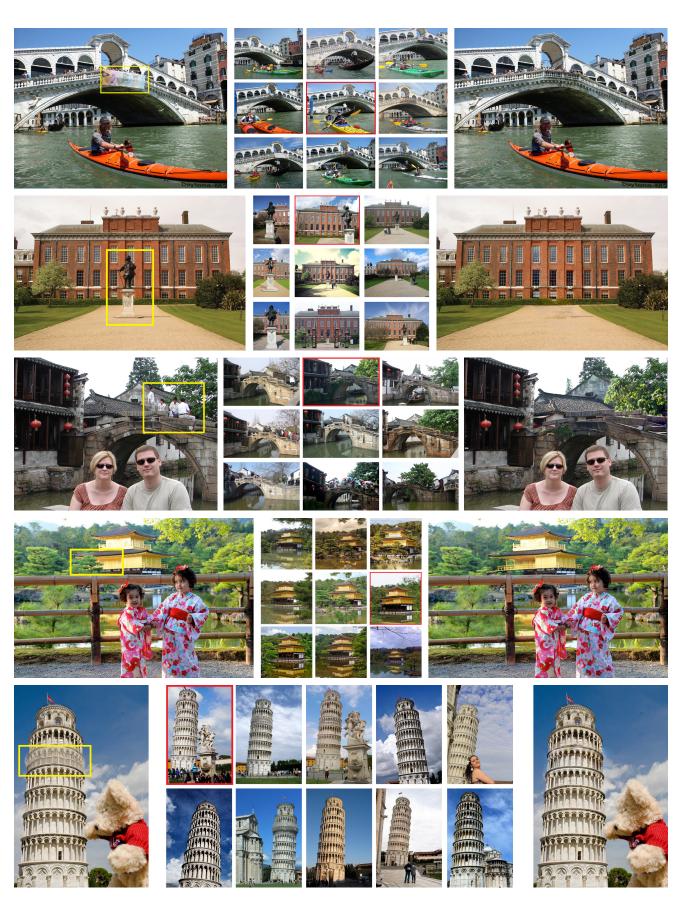


Fig. 6. Further completion results. Left: image to be completed; yellow rectangles mark the regions to be completed. Middle: candidate images. Right: completion result.



Fig. 8. Comparison to scene completion [4] and PatchNet [5].

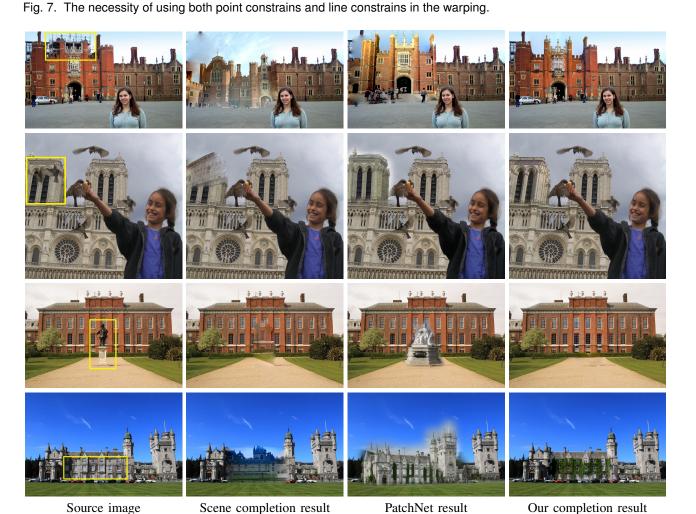
#### 9 **CONCLUSIONS AND FUTURE WORK**

We have proposed an approach for faithful completion of scenic landmark images using Internet images. The input comprises an image, a user given text label naming the landmark, and a region mask indicating where the image is to be completed. The completion process is fully automatic. Our method first downloads thousands of images from the Internet using the provided text label, and reduces them to a small set of candidate images through two-step filtering. For each candidate image, we apply co-matching to find point and line matches between the input image and the candidate, and compute a warp relating it to the input image.

A completion result is obtained through gradient domain blending. The completion results with highest combination scores, which consider both warping and blending energy, are then displayed to users. We have validated our approach on many famous landmarks; experiments show that our approach can generate faithful results in most cases.

In future, to improve result quality, we plan to add an additional color transfer step to deal with cases when there are large tone and illumination differences between the input and candidate images. We also plan to extend our warping method to more general cases, such as adding support for panoramas.

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(a)

Source image



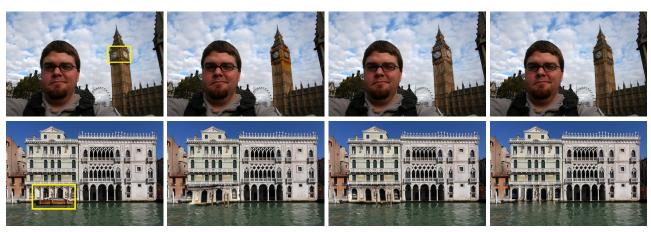


(c)

Result without point constrains Result without line constrains Result with both constrains



Our completion result



Source image

With point correspondence

With line correspondence

Our completion result

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Fig. 9. Comparison with moving least squares deformation (MLSD) [50].



Source image

Single homography

Multiple homography

Our completion result

Fig. 10. Comparison with single homography [8] and multiple homography [7] approaches.

## ACKNOWLEDGMENT

This work was supported by the National High Technology Research and Development Program of China (Project Number 2013AA013903) and the Natural Science Foundation of China (Project Number 61272226/61170153/61120106007), Research Grant of Beijing Higher Institution Engineering Research Center, and Tsinghua University Initiative Scientific Research Program.

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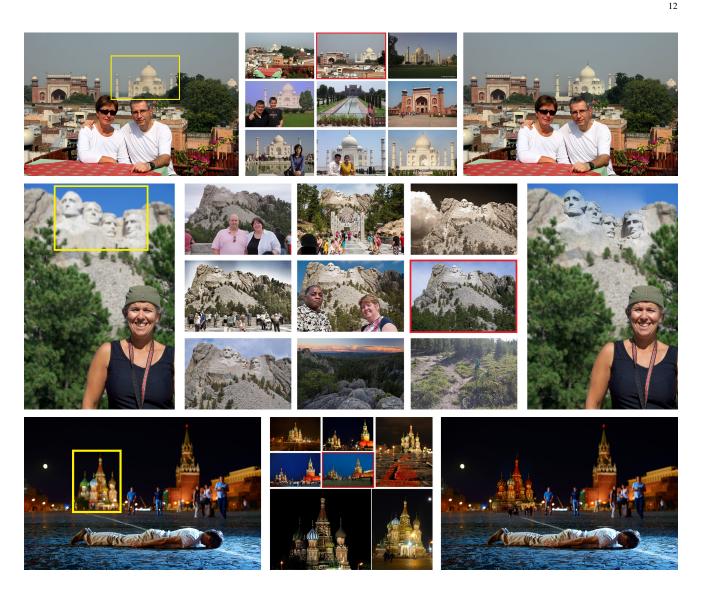


Fig. 11. Increasing the depth of field.

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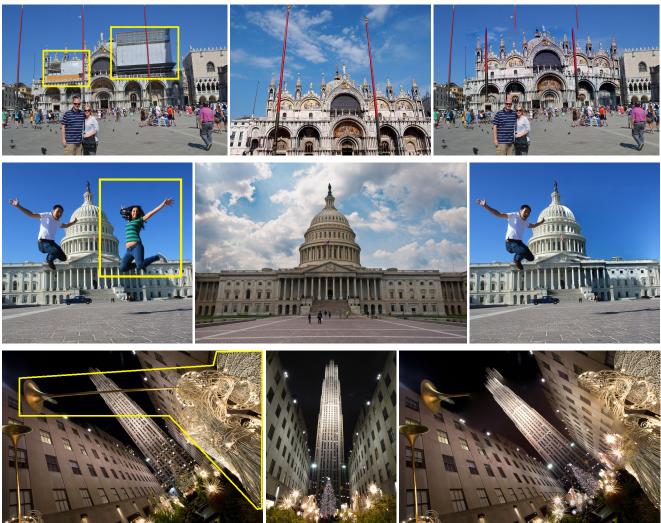


Fig. 12. Failures. Left: input image. Middle: candidate image. Right: completion result.

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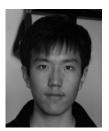
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